## A Survey of Inelastic Neutron Scattering

- Properties of the neutron
- The neutron scattering cross section

• The triple axis spectrometer

- Phonons
- Time-of-flight spectrometry
- Experimental details



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**Neutrons:** no charge spin = 1/2massive: mc<sup>2</sup>~IGeV 235**U** + n daughter nuclei 2-3 n +  $\gamma$ s

# The Neutron as a Wave

Energy, wave vector, wavelength, velocity :

$$k = \frac{m_n v}{\hbar} = \frac{2\pi}{\lambda} \qquad E = k_B T = 0.08617 \, mev \cdot K^{-1} \times T$$

$$E = \frac{\hbar^2 k^2}{2m_n} = \frac{\hbar^2}{2m_n} (\frac{2\pi}{\lambda})^2 = \frac{81.81 \, mev \cdot \mathring{A}^2}{\lambda^2}$$

Neutrons with λ typical of interatomic spacings (~ 2 Å) have energies typical of elementary excitations in solids (~ 20 meV)

#### What are we typically trying to understand?



What is the atomic and magnetic structure of new materials? What are the dynamic properties of the atoms and the magnetic moments?

• How are structure and dynamics related to physical properties?

### The Basic Neutron Scattering Experiment







#### **Incident Beam**

#### **Scattered Beam**

- Monochomatic
- "White"
- "Pink"

- Resolve its energy
- Don't resolve its energy
- Filter its energy

## Fermi's Golden Rule within the 1st Born approximation



## Neutrons scatter off nuclei



#### Dipole moment of the neutron interacts with the magnetic field generated by the electron



Dipole field due to orbital currents Dipole field due to Spin of the electron(s)





 $2\pi$ 

a







**Bragg diffraction** 

constructive interference when

$$\vec{Q} = \vec{k}_i - \vec{k}_f = \vec{\tau}$$

= a reciprocal lattice vector



# **Elementary Excitations**



# **Phonon Polarizations**

#### 



**Transverse Acoustic** 

#### **Transverse Acoustic**



• • • • • • •

**Transverse Optic** 

### Phonon eigenvectors and eigenvalues



#### Momentum $Q = k_i - k_f$

# Phonons in 3D



## Phonons in more complicated 3D structures



Chaplot, et al., Phys. Rev. B 52, 7230(1995).

#### KBr - two atoms/unit cell

#### 3 acoustic phonon branches 3 optic phonon branches

#### La<sub>2</sub>CuO<sub>4</sub> many atoms/unit cell

3 acoustic phonon branches 3n-3 = many optic phonon branches











## Two different ways of performing constant-Q scans

 $\mathbf{Q} = \mathbf{k}_i - \mathbf{k}_f$ 









#### Mapping Momentum (Q) and Energy ( $\hbar\omega$ ) space



# Putting the Q-map of the scattering with the reciprocal lattice of the crystal





# Putting the Q-map of the scattering with the reciprocal lattice of the crystal





# Constant-Q triple axis data



# Constant-E triple axis data



# **QR code for NXS Survey**

Lecture – 9:45 – 10:45

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https://forms.office.com/g/ASnB2UY2xT



The coherent neutron scattering cross section for phonons

$$S(\vec{Q},\hbar\omega) = \frac{1}{2NM} e^{-Q^2 \langle u^2 \rangle} \sum_{j,\vec{q}} |\vec{Q} \cdot \vec{\varepsilon}_j(\vec{q})|^2 \frac{1}{\omega_j(\vec{q})}$$

The displacement (eigenvectors) of the atoms must be // to the momentum transfer

× 
$$(1 + n(\hbar\omega))$$
  $\delta(\vec{Q} - \vec{q} - \vec{\tau})$   $\delta(\hbar\omega - \hbar\omega_j(\vec{q}))$ 

The neutron can always create a phonon, but it cannot destroy a phonon unless one is already present

Momentum must be conserved Energy must be conserved

# The coherent neutron scattering cross section for phonons





Longitudinal scan, q || ε

Transverse scan,  $\mathbf{q} \perp \epsilon$ 

$$S(\vec{Q},\hbar\omega) = \frac{1}{2NM} e^{-Q^2 \langle u^2 \rangle} \sum_{j,\vec{q}} |\vec{Q} \cdot \vec{\varepsilon}_j(\vec{q})|^2 \frac{1}{\omega_j(\vec{q})}$$
  
×  $(1+n(\hbar\omega)) \quad \delta(\vec{Q}-\vec{q}-\vec{\tau}) \quad \delta(\hbar\omega-\hbar\omega_j(\vec{q}))$ 

# The coherent neutron scattering cross section for phonons



### **Time-of-flight Neutron Scattering**

#### Neutrons have *mass* so higher energy means faster – lower energy means slower

15 30 K flux(v) in arb. units 10 5 300 K 3000 K 5 10 v (km/sec)

 $v (km/sec) = 3.96 / \lambda (A)$ 

- 4 A neutrons move at  $\sim 1$  km/sec
- DCS: 4 m from sample to detector
- It takes 4 msec for elastically scattered 4 A neutrons to travel 4 m
- msec timing of neutrons is easy
- $\delta E / E \sim 1-3 \%$  very good !

We can measure a neutron's energy, wavelength by measuring its speed

#### **Time-of-flight Neutron Scattering**



#### **Time-of-flight Neutron Scattering**



### Time-of-flight Neutron Scattering: Disc Choppers

A single (disk) chopper pulses the neutron beam.



A second chopper selects neutrons within a narrow range of speeds.



Counter-rotating choppers (close together), with speed  $\bullet$ , behave like single choppers with speed 2 $\bullet$ . They can also permit a choice of pulse widths.

Additional choppers remove "contaminant" wavelengths and reduce the pulse frequency at the sample position.

### Time-of-flight Neutron Scattering: Disc Choppers

The DCS has seven choppers, 4 of which have 3 "slots"



### **Time-of-flight Neutron Scattering: Fermi Choppers**





# 4D data sets for single crystals can be very large ~ 2 Tbyte



# **Resolution Considerations**

Resolution "ellipse" is defined by:

Beam divergences
Collimation and distances
Crystal mosaic, sizes
Beam energy



 $I(\vec{Q}_0,\hbar\omega_0) = \int S(\vec{Q}_0 - \vec{Q},\hbar\omega_0 - \hbar\omega) R(\vec{Q}_0,\hbar\omega_0) d\vec{Q} d\hbar\omega$ 









Q or angular resolution improved by using collimation (Soller slits)



Allows the *angular* resolution of **k**<sub>i</sub>, **k**<sub>f</sub> to be selected

#### Harmonic contamination from crystal monochromators



# Neutron filters remove $\lambda/n$ from incident or scattered beam, or both.



### Harmonic contamination from crystal monochromators: Pyrolitic Graphite



# **Neutron Detectors**

#### **Gas Detectors**

- n + <sup>3</sup>He → <sup>3</sup>H + p + 0.764 MeV
- ionization of gas
- high efficiency



#### Beam monitors low efficiency detectors for monitoring beam flux





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